SA305 – Linear Programming Asst. Prof. Nelson Uhan

## Lesson 21. The Simplex Method – Example

Problem 1. Consider the following LP

maximize 
$$4x_1 + 3x_2 + 5x_3$$
  
subject to  $2x_1 - x_2 + 4x_3 \le 18$   
 $4x_1 + 2x_2 + 5x_3 \le 10$   
 $x_1, x_2, x_3 \ge 0$ 
(1)

The canonical form of this LP is

maximize 
$$4x_1 + 3x_2 + 5x_3$$
  
subject to  $2x_1 - x_2 + 4x_3 + s_1 = 18$   
 $4x_1 + 2x_2 + 5x_3 + s_2 = 10$   
 $x_1, x_2, x_3, s_1, s_2 \ge 0$ 
(2)

- a. Use the simplex method to solve the canonical form LP (2). In particular:
  - Use the initial BFS  $\mathbf{x}^0 = (0, 0, 0, 18, 10)$  with basis  $\mathcal{B}^0 = \{s_1, s_2\}$ .
  - Choose your entering variable using **Dantzig's rule** that is, choose the improving simplex direction with the most positive reduced cost. (If this was a minimization LP, you would choose the improving simplex direction with the most negative reduced cost.)
- b. What is the optimal value of the canonical form LP (2)? Give an optimal solution.
- c. What is the optimal value of the original LP (1)? Give an optimal solution.

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Spring 2016