## Calculus III with Optimization

Textbook: Calculus: Early Transcendentals, 8th edition, by James Stewart
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## SM223 (Fall 2021): Syllabus

1. Three dimensional space
2. Vectors
3. Dot Product
4. Dot Product
5. Cross Product
6. Cross Product
7. Lines and Planes
8. Lines and Planes
9. Lines and Planes
10. Cylinders and Quadric Surfaces
11. Cylinders and Quadric Surfaces
12. Review
13. Test \#1
14. Vector Functions
15. Vector Functions
16. Derivatives and Integrals
17. Arc Length (no curvature)
18. Motion in Space
19. Motion in Space
20. Functions of Many Variables
21. Functions of Many Variables
22. Functions of Many Variables
23. Partial Derivatives
24. Partial Derivatives
25. Partial Derivatives
26. Partial Derivatives
27. Review
28. Test \#2
29. Tangent Planes and Linear Approximation
30. Tangent Planes and Linear Approximation
31. Chain Rule
32. Chain Rule
33. Chain Rule
34. Gradients and Directional Derivative
35. Gradients and Directional Derivative
36. Gradients and Directional Derivative
37. Max-Min
38. Max-Min
39. Lagrange Multipliers
40. Lagrange Multipliers
$12.1 \quad \# 5,9,12,15,17,27,31,35$
$12.2 \quad \# 3,13,19,21,25,37$
$12.3 \quad \# 7,9,11,15,23$
$12.3 \quad \# 33,35,39,41,49,55$
$12.4 \quad \# 3,9,13,14,19$
$12.4 \quad \# 27,31,33,37$
$12.5 \quad \# 3,4,7,10,13$
$12.5 \quad \# 16,19,23,26,27$
$12.5 \quad \# 31,35,45,51,67$
12.6 \# 1, 3, 5, 11, 17
12.6 \# 21-28
$13.1 \# 7,9,15,16,18$
13.1 \# 21-26
$13.2 \# 3,5,15,19,25,28,29,34$
13.3 \# 1, 3, 5, 9
13.4 \# 5, 9, 13, 15, 18
13.4 \# 19, 23, 25, 31, 35
14.1 \# 1, 3, 7, 24, 25
$14.1 \quad \# 32,35,36,41,44$
$14.1 \quad \# 46,61-66,68,69$
$14.3 \quad \# 3,4,5,7,8,10$
14.3 \# 11, 15, 17, 18, 20
$14.3 \quad \# 22,26,33,34,41,42$
$14.3 \# 53,56,64,66,74,82$

| 14.4 | $\# 1,2,4,5,6$ |
| :--- | :--- |
| 14.4 | $\# 21,24,25,27$ |
| 14.5 | $\# 1,2,11,13,14,35$ |
| 14.5 | $\# 3,4,15,37,38$ |
| 14.5 | $\# 5,6,39,40,41$ |
| 14.6 | $\# 1,3,7,9,13,15$ |
| 14.6 | $\# 19,21,23,29,31$ |
| 14.6 | $\# 31,33,38,41,45,49,55$ |
| 14.7 | $\# 3,5,6,11,41$ |
| 14.7 | $\# 4,12,13,45,49$ |
| 14.8 | $\# 3,5,7,9$ |
| 14.8 | $\# 19,31,33,35$ |

$14.4 \quad \# 1,2,4,5,6$
$14.4 \quad \# 21,24,25,27$
$14.5 \quad \#$ 1, 2, 11, 13, 14, 35
$14.5 \quad \# 3,4,15,37,38$
$14.5 \quad \# 5,6,39,40,41$
$14.6 \quad \# 1,3,7,9,13,15$
14.6 \# 19, 21, 23, 29, 31
\# 31, 33, 38, 41, 45, 49, 55

- $3,5,6,11,4$
$14.8 \quad \# 3,5,7,9$
$14.8 \quad \# 19,31,33,35$

| 41. | Lagrange Multipliers | 14.8 | $\# 21,39,45$ |
| :--- | :--- | :--- | :--- |
| 42. | Review |  |  |
| 43. | Test \#3 |  |  |
| 44. | Double Integration over Rectangular Regions | 15.1 | $\# 1,5,7,15,17$ |
| 45. | Double Integration over Rectangular Regions | 15.1 | $\# 8,19,21,27,28$ |
| 46. | Double Integration over General Regions | 15.2 | $\# 1,7,13,15,17$ |
| 47. | Double Integration over General Regions | 15.2 | $\# 19,21,27,28,45,49$ |
| 48. | Double Integration over Polar Coordinates | 15.3 | $\# 5,7,8,9,10,11$ |
| 49. | Double Integration over Polar Coordinates | 15.3 | $\# 12,15,29,31,32$ |
| 50. | Applications | 15.4 | $\# 3,7,11,13$ |
| 51. | Application | 15.4 | $\# 27,28,29$ |
| 52. | Triple Integrals | 15.6 | $\# 4,5,13,14,19$ |
| 53. | Triple Integrals | 15.6 | $\# 27,28,33,35$ |
| 54. | Triple Integrals over Cylindrical Coordinates | 15.7 | $\# 1,3,9,17$ |
| 55. | Triple Integrals over Cylindrical Coordinates | 15.7 | $\# 18,23,24,29$ |
| 56. | Triple Integrals over Spherical Coordinates | 15.8 | $\# 1,3,5,6,9$ |
| 57. | Triple Integrals over Spherical Coordinates | 15.8 | $\# 17,19,21,25,30,41$ |
| 58. | Review |  |  |
| 59. | Test \#4 |  |  |
| 60. | Review |  |  |

41. Lagrange Multipliers
$\begin{array}{llll}\text { 44. } & \text { Double Integration over Rectangular Regions } & 15.1 & \# 1,5,7,15,17 \\ \text { 45. } & \text { Double Integration over Rectangular Regions } & 15.1 & \# 8,19,21,27,28\end{array}$
42. Double Integration over General Regions $\quad 15.2 \quad \# 1,7,13,15,17$
43. Double Integration over General Regions $\quad 15.2 \quad \# 19,21,27,28,45,49$
44. Double Integration over Polar Coordinates $\quad 15.3 \quad \# 5,7,8,9,10,11$
45. Double Integration over Polar Coordinates $\quad 15.3 \quad \# 12,15,29,31,32$
46. Applications
$15.4 \# 3,7,11,13$
47. Application
48. Triple Integrals
$15.6 \quad \# 4,5,13,14,19$
15.6 \# 27, 28, 33, 35
49. Triple Integrals over Cylindrical Coordinates
\# 1, 3, 9, 17
Triple Integrals over Cylindrical Coordinate
\# 1, 3, 5, 6, 9
50. Triple Integrals over Spherical Coordinates $\quad 15.8 \quad \# 17,19,21,25,30,41$
51. Review
52. Review

The final exam will consist of a multiple choice section and a long answer section.

Course Goals: Upon successful completion of this course, midshipmen will be able to do the following:

1. Describe basic curves and space motion (including projectile motion) using vector functions and their derivatives and integrals
2. Draw and interpret level sets and graphs of a real valued function
3. Use partial derivatives, directional derivatives, and gradient vectors to describe the behavior of a real valued function.
4. Solve extreme value problems by finding and classifying critical points and by the method of Lagrange multipliers
5. Evaluate double and triple integrals in rectangular and polar coordinates and use integrals to find centers of mass and probabilities
6. Write well-organized, coherent solutions to applications problems
